

EMRI kludges:

What they are, why they're important, and how to end them

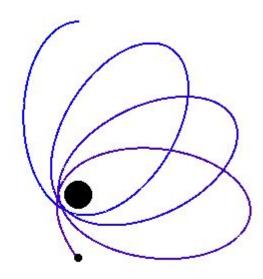
Alvin Chua

22nd Capra Meeting CBPF, Rio de Janeiro 17 June 2019



Outline

- What's a kludge?
- An inventory of EMRI kludges
 - Analytic kludge (AK)
 - Numerical kludge (NK)
 - Augmented analytic kludge (AAK)
- Kludges in LISA preparatory science
- The EMRI data analysis problem
- Paving the way to surrogates
 - Existing pieces
 - Compression & interpolation
 - Strategies & coordination



What's a kludge?

Some particularly apt dictionary definitions:

"Any construction or practice, typically crude yet effective, designed to solve a problem temporarily or expediently"



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"Any construction or practice, typically crude yet effective, designed to solve a problem temporarily or expediently"

"An ill-assorted collection of poorly matching parts, forming a distressing whole"

"A badly written or makeshift piece of software"



What's an EMRI kludge model?

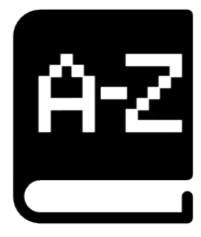
- if Efficiency-oriented
 - Feasible for bulk use in data analysis algorithms
- and End-to-end
 - \circ Source parameters \rightarrow trajectory \rightarrow orbit \rightarrow waveform \rightarrow detector response
- and Extensive
 - Describes generic Kerr orbits (intrinsic) & observer dependence (extrinsic)
- and not Fully relativistic
 - At least one component uses flat-space approximation
- then It's a kludge!

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- then It's a kludge!
- Disclaimer: This is my personal, completely non-standard definition
 - But really the only one you should use

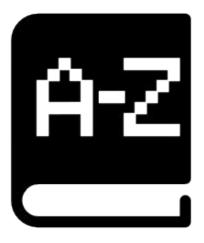
While we're defining terms...

- Waveform model:
 - Not efficiency-oriented + fully relativistic
- Template model:
 - Efficiency-oriented + end-to-end + extensive

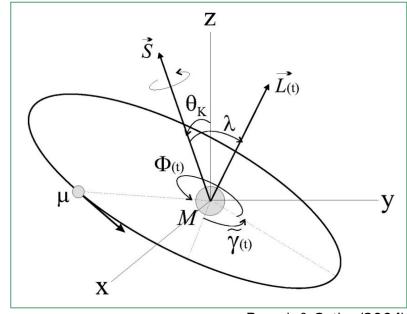


While we're defining terms...

- Waveform model:
 - Not efficiency-oriented + fully relativistic
- Template model:
 - Efficiency-oriented + end-to-end + extensive
- Surrogate model:
 - Efficiency-oriented + end-to-end + extensive + fully relativistic
 - o i.e., a surrogate is a template model that is not a kludge
 - o Can (probably will) be phenomenological, not self-consistent
 - Nomenclature is compatible with the NR ROM surrogates
- Approximant:
 - LIGO-speak for a surrogate

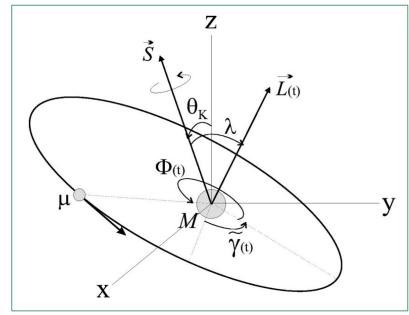


- Barack & Cutler, 2004
- PN inspiral trajectory
 - Mixed-order fluxes for (p,e)
 - Assume constant inclination
- Flat-space orbital evolution
 - Instantaneous Keplerian ellipses
 - Add PN precession



Barack & Cutler (2004)

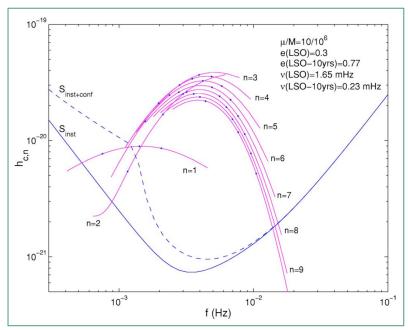
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- Flat-space waveform generation
 - o Peters-Mathews decomposition
 - Hence quadrupolar
- Time-domain detector response
 - Long-wavelength approximation
 - Extended to t/f rigid-equal-arm TDI (Babak)



Barack & Cutler (2004)

Strengths:

- Fast to generate at low eccentricity (< 0.5)
- Fast to generate for long signals
- Constructed from harmonic decomposition



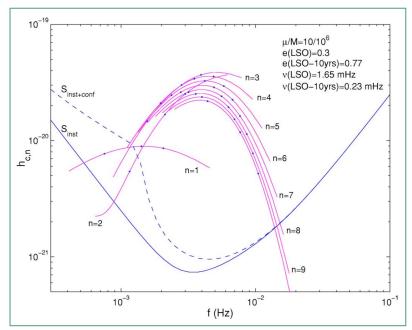
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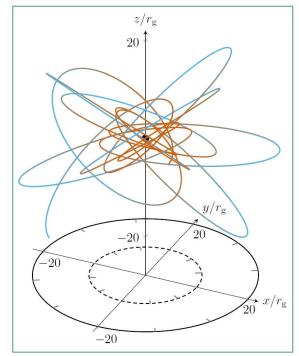
Weaknesses:

- Unphysical instantaneous frequencies
- Limited performance at high eccentricity



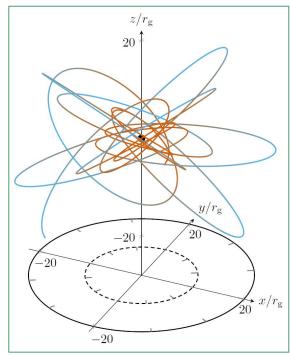
Barack & Cutler (2004)

- Babak et al., 2007
- PN inspiral trajectory
 - Mixed-order fluxes for (p,e,i)
 - Fit to adiabatic trajectories
- Curved-space orbital evolution
 - Instantaneous Kerr geodesics
 - o Precession naturally included



Berry et al. (2019)

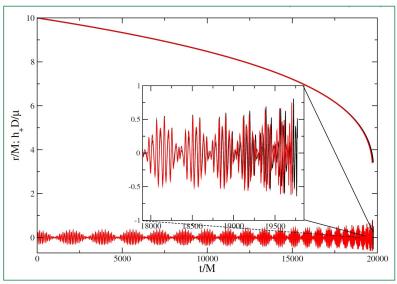
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 - Precession naturally included
- Flat-space waveform generation
 - Associate curved & flat coordinates
 - Several multipolar prescriptions
- Time-domain detector response
 - Only long-wavelength approximation
 - Needs LISA simulator for accurate response



Berry et al. (2019)

• Strengths:

- Good agreement with Teukolsky waveforms
- Much faster than relativistic models
- Easy to incorporate better trajectories



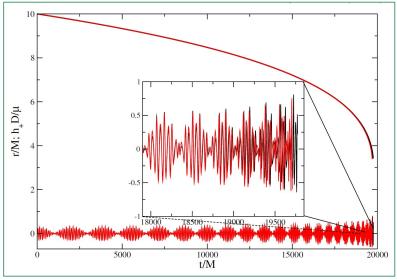
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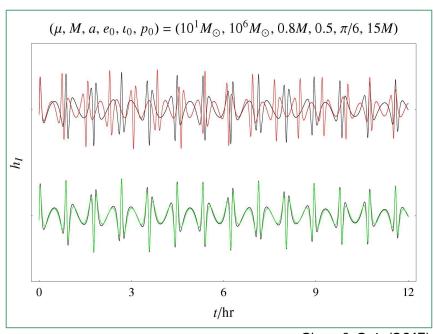
Weaknesses:

- Multipole formalism is inefficient
- Weak-field approximation is inaccurate at high eccentricity (see talk by Osburn)
- No easy harmonic decomposition



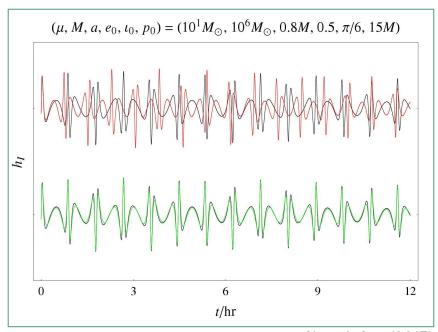
Babak et al. (2007)

- Chua & Gair, 2015
- PN inspiral trajectory
 - 3PN O(e^6) fluxes for (p,e)
 - Assume constant inclination
 - Local fit to NK trajectories
- Flat-space orbital evolution
 - Map to Kerr instantaneous frequencies
 - Otherwise same as AK



Chua & Gair (2015)

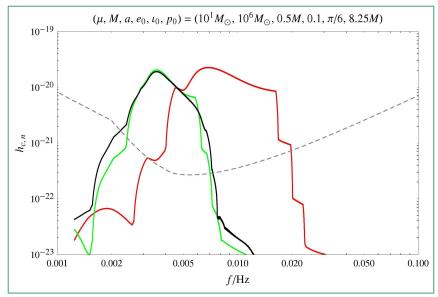
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- Flat-space waveform generation
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Strengths:

- Same as AK
- Good agreement with NK waveforms
- Improved implementation
- Actually being maintained by postdoc



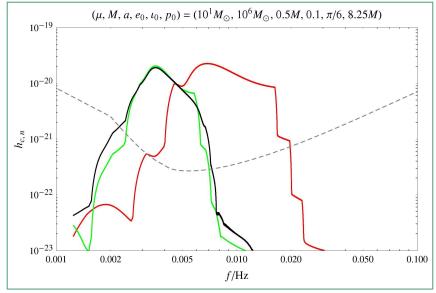
Chua, Moore & Gair (2017)

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Weaknesses:

- Limited performance at high eccentricity
- Frequency map ill-defined at plunge



Chua, Moore & Gair (2017)

- Software suite with all 3 kludges & common interface
 - Latest version: 0.4.2
 - NK not being maintained
 - AK only being maintained until end of LDC-1



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Installation

- Clone from: github.com/alvincjk/EMRI_Kludge_Suite
- Needs GSL & FFTW libraries
- Python wrapper available for some executables



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Usage

- Executables in ./bin: Waveforms (all models), TDIs (AK/AAK), phases (AAK)
- Template files in ./examples: Source/waveform parameters, model settings
- Import Python module AAKwrapper, example usage in AAKdemo.py
- Caveat utilitor: Limited domain validation & error handling



Model	Trajectory	Orbit	Waveform/response	Accuracy	Speed
AK	- Mixed-order PN fluxes	- Evolving Keplerian ellipses	- Peters-Mathews approximation to quadrupole - Rigid-equal-arm approximation (TDIs)	- Instantaneous frequencies too high - Schwarzschild plunge handling - Qualitative use only	- Fast, but less speedup over NK for shorter waveforms or more eccentric orbits
AAK	- 3PN O(e^6) fluxes - Locally fitted to NK trajectories	- Evolving Keplerian ellipses - Instantaneous frequencies mapped to Kerr	- Peters-Mathews approximation to quadrupole - Rigid-equal-arm approximation (TDIs)	- Phase-accurate w.r.t. NK waveforms, for 2-6 months - Approximate Kerr plunge handling	- Same as AK, but slightly faster due to streamlining
NK	- Mixed-order PN fluxes - Fitted to adiabatic trajectories	- Evolving Kerr geodesics	- Quadrupole - Long-wavelength approximation (h_I,II)	- Phase-accurate w.r.t. adiabatic waveforms, down to 2-3 r_ISCO - Kerr plunge handling	- Order of magnitude slower than AK/AAK on average



- Data analysis
 - Synthetic data sets
 - MLDCs, 2006-2011 (using AK); LDCs, 2018-present (transitioning from AK to AAK)
 - Search algorithms
 - Babak, Gair & Porter, 2009 + Cornish, 2011 + Wang, Shang & Babak, 2012 + several others (all using simplified, kludge-informed, time-frequency techniques)
 - Inference algorithms
 - Ali et al., 2012 (short data segments); not much else (even kludges are still too slow)



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 - Degeneracies & confusion
 - Chua & Cutler, in prep. (mapping out the overlap surface); Barack & Cutler, 2004 + Karnesis, Chua & Babak, in prep. (unresolvable EMRI background)
 - Systematics (theoretical errors)
 - Huerta & Gair, 2009 (effect of conservative corrections); Berry et al., 2016 (effect of resonances); Chua et al., in prep. (error marginalization)



- Mission performance
 - Detection rates
 - Gair et al., 2004 (using AK); Babak et al., 2017 + several other reports/proposals (still using AK); Chua, Moore & Gair, 2017 (using AAK)
 - Parameter estimation precision (statistical errors)
 - Barack & Cutler, 2004 + Babak et al., 2017 + several other reports/proposals (all using AK)



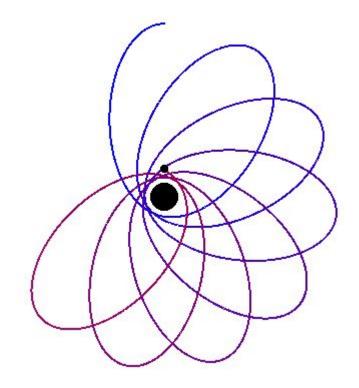
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Science applications

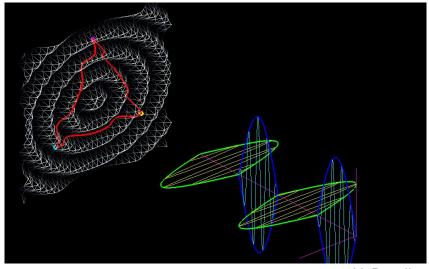
- Fundamental physics (tests of gravity)
 - Glampedakis & Babak, 2006 + Barack & Cutler, 2007 + Chua et al., 2018 (generic Kerr deviations); Canizares, Gair & Sopuerta, 2012 (dynamical Chern-Simons); possibly others
- Astrophysics & cosmology
 - Sesana et al., 2008 (WD EMRIs); Han & Chen, 2019 (b-EMRIs);
 surprisingly not much else (heuristic analysis, or just use cited rates/precision)

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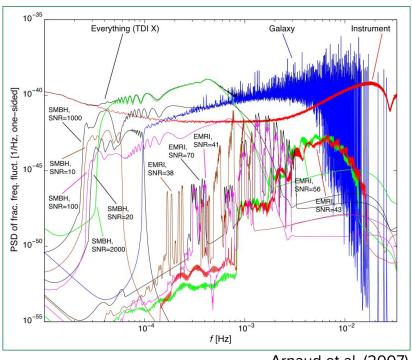


- Problem 0: Instrument/noise model
 - Complicated instrument response
 - Non-stationary noise
 - Gaps & glitches



N. Douillet

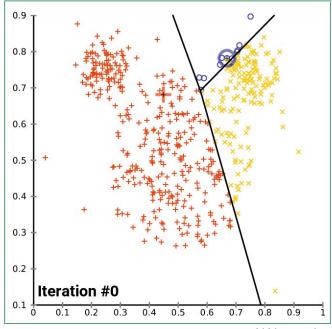
- Problem 0: Instrument/noise model
 - Complicated instrument response
 - Non-stationary noise
 - Gaps & glitches
- Problem 1: Signal confusion
 - Many signals overlap in time/frequency:
 Galactic binaries + SMBH mergers + EMRIs
 - Cannot just subtract then move on
 - Global-solution algorithm is required
 - Not practical to do fully simultaneous fit



Arnaud et al. (2007)

Problem 2: Global search

- Parameter space can be massive:
 Large dimensionality & information volume
- Credible regions can be very localized
- Stochastic search algorithms are required
- Search is hierarchical & needs multiple passes



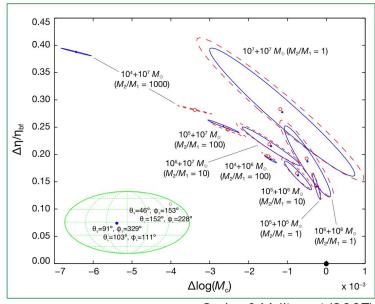
Wikimedia

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Problem 3: Modeling accuracy

- Bias when theoretical error > statistical error
- Only for strong-field, high-SNR sources
- Most interesting, but most difficult to model
- Need to understand errors for waveforms,
 minimize loss of accuracy for templates



Cutler & Vallisneri (2007)

The EMRI data analysis problem

Galactic binaries

- Confusion: Severe (resolvable + background)
- Search: Low SNR & many signals to resolve, but templates are inexpensive
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EMRIs

- Confusion: Maybe (possible degeneracies, uncertain event rates)
- Search: Expensive templates, highly localized, moderate SNR, possibly many signals
- Modeling: Difficult (SF)



















Will kludges be good enough?

In terms of speed

- Template cost: $> 10^2$ s (!)
- \circ Time samples: > 10^7 (4 years × 0.1 Hz)
- Overlap calls: 10⁹-10³⁰ (!!)
- Prohibitive for search (without sacrificing accuracy)
- Barely OK for inference



ORNL

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In terms of accuracy

- Assume overlaps of 0.97 with true signals
- Barely OK for search: Lose up to half of signals (Chua, Moore & Gair, 2017)
- Nowhere near good enough for inference



ORNL

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Let's leave kludges & traditional data analysis approaches behind

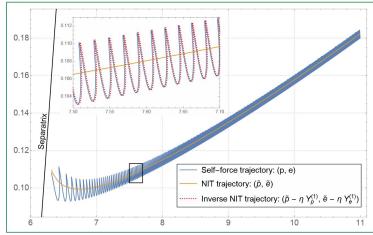


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Surrogates: Existing pieces

Trajectory & orbit

- PN flux-based (see talks by Isoyama, Munna)
- Teukolsky flux-based (see talk by Hughes)
- SF-based (van de Meent & Warburton, 2018;
 see also talk by Osburn)



van de Meent & Warburton (2018)

Surrogates: Existing pieces

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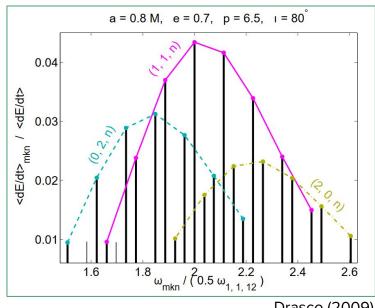
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Waveform

- Teukolsky snapshots
- Adiabatic (see talks by Hughes, Isoyama)

Response

Approximate TDI (Babak; Marsat & Baker, 2018)



Drasco (2009)

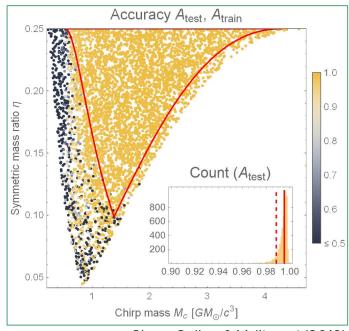
Surrogates: Compression & interpolation

- ROM surrogates (Field et al., 2014)
 - Construct reduced basis for signal space
 - Only valid over restricted parameter domain
 - Resultant template model is fast & accurate
 - May be viable for EMRIs with smart representation

$$h(\theta) = \sum_{i} \alpha_{i}(\theta) e_{i} \equiv \alpha(\theta)$$

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 - Construct reduced basis for signal space
 - Only valid over restricted parameter domain
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 - May be viable for EMRIs with smart representation
- ROMAN (Chua, Galley & Vallisneri, 2019)
 - Same basis & domain as ROM surrogates
 - Comparable speed & accuracy
 - More general, connects directly to data analysis
 - Shows utility of neural-network interpolation (dimensionality, derivatives, etc.)

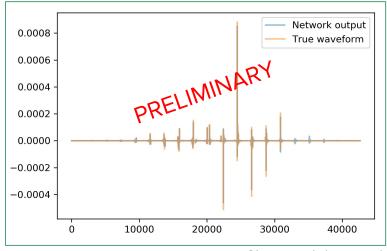


Chua, Galley & Vallisneri (2019)

- Work in time-frequency domain
 - Lossless representation: STFT, wavelets, etc.
 - Admits native generation & data analysis
 - o Can deal with non-stationarity & gaps
 - Best suited to nature of EMRIs & LISA

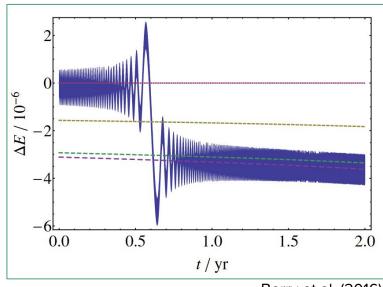
$$h(\tau,\omega) = \int dt \, h(t)W(t-\tau)e^{-i\omega t}$$
$$h(a,b) = \frac{1}{\sqrt{a}} \int dt \, h(t)\psi\left(\frac{t-b}{a}\right)$$

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 - o e.g. Map geodesics to Teukolsky amplitudes
- Incorporate parallelization from the start
 - e.g. Native GPU implementations



Chua et al. (in prep.)

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 - o e.g. Map geodesics to Teukolsky amplitudes
- Incorporate parallelization from the start
 - e.g. Native GPU implementations
- Identify & add important missing pieces
 - Transient resonances
 - Tidal resonances? (see talk by Bonga)
 - Secondary spin? (see talk by Witzany)



Berry et al. (2016)

- LSG WP 1.8.3: Efficient EMRI models
 - Kludges & related tools for LDCs
 - Fast LISA response for EMRIs
 - Reduced-representation templates
 - Fast transient resonance models
 - Fast SF trajectories
 - Modern computational techniques
- Also WPs 1.2.1 (Pound), 1.2.2 (Warburton), 1.2.3 (Brito)



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- Also WPs 1.2.1 (Pound), 1.2.2 (Warburton), 1.2.3 (Brito)
- Calling for expressions of interest/commitment
 - No need to be full or even associate LISA member
 - More at: tinyurl.com/emri-templates



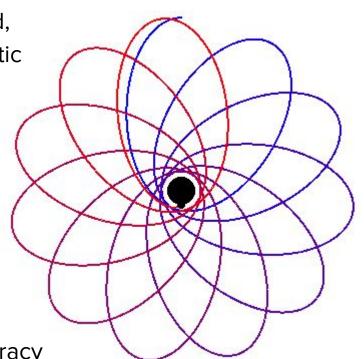
Summary

 EMRI kludge models are efficiency-oriented, end-to-end, extensive, but not fully relativistic

 Kludges have fulfilled their purpose of scoping out LISA data analysis issues; they will still be relevant in the near future

 We now have the pieces to construct surrogate models that are more directly informed by perturbation theory

 These will be tailored to LISA data analysis requirements; modern computational techniques will improve both speed & accuracy



References

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